

Seminar 1- Introduction to the course and review of main mathematical terms

Program of the Seminar:

1. Rules and Demands for the Course (attached files)
2. Introduction to the Econometrics discipline
3. Review of terms
 - a. Matrix algebra
 - b. Differentiations

Practical tasks:

1. Write down an arbitrary column vector and create its transposition.
2. Carry out a scalar product of the vector. What is the result of the operation?
3. Carry out following operations and decide if the product will be a vector or a scalar.

$$\begin{matrix} 3 & 7 \\ 2-5+31 & = \\ 4 & 2 \end{matrix}$$

4. Write down an arbitrary matrix of 2*3 and another matrix of the same size. Carry out their addition.
5. If possible, carry out an addition of the following matrices:

$$\begin{matrix} 1 & 4 & 3 & 5 & 7 \\ 5 & 7 & 2 & 1 & 3 \end{matrix} + 2 =$$

6. Determine the matrix size of the following operations:

$$\begin{matrix} 3 \times 5 & \times & 5 \times 2 & = \\ 2 \times 3 & \times & 2 \times 3 & = \\ 2 \times 1 & \times & 1 \times 5 & = \end{matrix}$$

7. Determine the resulting matrix size and if possible, carry out the product of the matrices:

$$\begin{matrix} \text{a) } A = \begin{matrix} 3 & -1 & 0 \\ 2 & 3 & 1 \end{matrix} & \times & B = \begin{matrix} 5 \\ 1 \\ 2 \end{matrix} \\ \text{b) } A = \begin{matrix} 4 & 3 \\ 2 & 6 \end{matrix} & \times & B = \begin{matrix} 2 & 4 \\ 4 & 2 \end{matrix} \\ \text{c) } A = \begin{matrix} 3 & 1 & 2 \\ -1 & 2 & 4 \end{matrix} & \times & B = \begin{matrix} 1 & 4 & -1 \\ 0 & 3 & 1 \end{matrix} \end{matrix}$$

8. Verify, if the commutative rule of multiplication ($AxB = BxA$) applies also for matrices (on the example of 7b).
9. Carry out multiplication of AxB and BxA and derive the rule for multiplication of square matrices.

$$\begin{array}{r}
 3 \ 0 \ 1 \\
 A = 2 \ 1 \ 0 \\
 2 \ 0 \ 1
 \end{array}
 \quad
 \times
 \quad
 \begin{array}{r}
 3 \ 2 \ 1 \\
 B = 1 \ 0 \ 2 \\
 3 \ 1 \ 0
 \end{array}$$

10. Carry out the inversion of the matrices and make a proof that your result is correct.

$$\text{a) } A = \begin{pmatrix} 3 & 2 \\ 1 & 3 \end{pmatrix} \quad A^{-1} =$$

$$\text{b) } B = \begin{pmatrix} 1 & 4 & 5 \\ 3 & 2 & 5 \\ 4 & 3 & 5 \end{pmatrix} \quad B^{-1} =$$

$$\text{c) } C = \begin{pmatrix} -1 & 3 \\ 4 & -2 \end{pmatrix} \quad C^{-1} =$$

11. Calculate the rank of the following matrices:

$$\text{a) } A = \begin{pmatrix} 0 & -3 & 1 & 0 \\ 0 & 0 & 2 & 1 \\ 2 & 3 & -1 & 0 \\ 3 & 2 & 1 & -4 \end{pmatrix} \quad B = \begin{pmatrix} 1 & 0 & 2 & 3 \\ -1 & 2 & 6 & 7 \\ -1 & 1 & 2 & 2 \\ -2 & 1 & 0 & -1 \end{pmatrix}$$

12. Carry out the derivatives of the following functions:

$$\text{a) } y = 2x^3 + 3x + 6$$

$$\text{b) } y = \sqrt{x} + 2\sqrt[2]{x^3}$$

$$\text{c) } y = 4x(2 + 5x^2)$$

$$\text{d) } y = (x^5 + 3x^2 - 2)^4$$

$$\text{e) } y = \frac{2x^3 + 3}{3x^2}$$

$$\text{f) } y = \frac{x^2 - 1}{x^2 + 1}$$

$$\text{g) } y = e^{5x}$$

$$\text{h) } y = xe^{4-x}$$

$$\text{i) } y = \ln x^2$$

$$\text{j) } y = (\ln x)^2$$

$$\text{k) } y = \ln(x^2 + 3x + 4)$$